

## End Semester Examination (2021-22)-Odd Semester

<b>M.Sc. (Physics) – I Year (I Sem)</b>	
<b>Course Name: Quantum Mechanics - I</b>	<b>Code: MPH1005</b>
<b>Time: 02 Hours</b>	<b>Max Marks: 60</b>

<b>University Roll No.</b>	
<b>(To be filled by the Student)</b>	

**Note: Please read instructions carefully:**

- a) The question paper has 03 sections and it is compulsory to attempt all sections.
- b) All questions of Section A are compulsory; questions in Section B and C contain choice.

<b>Section A: Very Short Answer type Questions</b>		<b>BL</b>	<b>CLO</b>	<b>Marks (10)</b>
<b>Attempt all the questions.</b>				
<b>1.</b>	Define reflection coefficient in potential step condition.	BL2	CLO2	02
<b>2.</b>	Write the condition for orthogonality of two wave functions.	BL1	CLO2	02
<b>3.</b>	Define quantum entanglement in quantum systems.	BL1	CLO4	02
<b>4.</b>	Illustrate the characteristics of a wave function.	BL2	CLO2	02
<b>5.</b>	State the condition of ortho normality of two vectors $ \Psi_1\rangle$ and $ \Psi_2\rangle$ .	BL1	CLO1	02
<b>Section B: Short Answer Type Questions</b>		<b>BL</b>	<b>CLO</b>	<b>Marks (30)</b>
<b>Attempt any 03 out of 06 questions.</b>				
<b>1.</b>	If $\Psi(x) = e^{ikx} + 2e^{-ikx}$ find probability current density.	BL3	CLO2	10
<b>2.</b>	Consider the states $ \Psi\rangle = 3i \Phi_1\rangle - 7i \Phi_2\rangle$ and $ x\rangle = - \Phi_1\rangle + 2i \Phi_2\rangle$ , where $ \Phi_1\rangle$ and $ \Phi_2\rangle$ are ortho normal. Calculate $ \langle\Psi x\rangle $ and $\langle\Psi x\rangle$ .	BL3	CLO1	10
<b>3.</b>	Consider the operator $A_x = -L_y p_z - L_z p_y$ , where $L_i$ and $p_i$ denote, respectively, the components of the angular momentum and momentum operators. Calculate commutator $[A_x, x]$ , where $x$ is the $x$ -component of the position operator.	BL4	CLO4	10
<b>4.</b>	If $\sigma_x$ , $\sigma_y$ and $\sigma_z$ are pauli's matrices, find the value expression $2\sigma_x\sigma_y + \sigma_y\sigma_x$ .	BL3	CLO2	10
<b>5.</b>	Find the value of $[L_z, P_x]$ .	BL4	CLO2	10
<b>6.</b>	Find the energy of the first excited quantum state of a particle in the two-dimensional potential $V(x, y) = \frac{1}{2}m\omega^2(x^2 + y^2)$ .	BL3	CLO3	10
<b>Section C: Long Answer Type Questions/Case Study</b>		<b>BL</b>	<b>CLO</b>	<b>Marks (20)</b>
<b>Attempt any 01 out of 03 questions.</b>				
<b>1.</b>	Derive an expression for energy of a infinite square potential well. Discuss the conditions under different energy conditions.	BL4	CLO3	20
<b>2.</b>	Explain various forms of the Uncertainty principle. Calculate the uncertainty of position ( $\Delta x$ ) and momentum ( $\Delta p$ ) of the particle represented by wave function $\Psi(x) = Ae^{ikx}$ .	BL3	CLO2	20
<b>3.</b>	Discuss different conditions for the validity of a wave function? The wave function of the particle is $\Psi(x) = \frac{1}{a}e^{-\frac{2 x }{a}}$ , $a > 0$ . Find the probability of finding the particle in the region $-a < x < a$ .	BL4	CLO4	20